

In general, a Clifford number transforms according to

$$(1) \quad \Phi \rightarrow \Phi' = \mathbf{R} \Phi \mathbf{S}$$

Clifford numbers

$$\text{e.g., } \mathbf{R} = e^{\frac{1}{2}\alpha^A \gamma_A}, \quad \mathbf{S} = e^{\frac{1}{2}\beta^A \gamma_A}$$

In particular, if  $\mathbf{S} = \mathbf{1}$ , we have

$$\Phi \rightarrow \Phi' = \mathbf{R} \Phi$$

As an example, let us consider the case

$$\mathbf{R} = e^{\frac{1}{2}\alpha \gamma_1 \gamma_2} = \cos \frac{\alpha}{2} + \gamma_1 \gamma_2 \sin \frac{\alpha}{2}, \quad \mathbf{S} = e^{\frac{1}{2}\beta \gamma_1 \gamma_2} = \cos \frac{\beta}{2} + \gamma_1 \gamma_2 \sin \frac{\beta}{2}$$

and examine, how various Clifford numbers,  $X = X^C \gamma_C$ , transform under (1), which now reads:

$$X \rightarrow X' = \mathbf{R} X \mathbf{S}$$

(i) If  $X = X^1 \gamma_1 + X^2 \gamma_2$

then

$$X' = X^1 \left( \gamma_1 \cos \frac{\alpha - \beta}{2} + \gamma_2 \sin \frac{\alpha - \beta}{2} \right) + X^2 \left( -\gamma_1 \sin \frac{\alpha - \beta}{2} + \gamma_2 \cos \frac{\alpha - \beta}{2} \right)$$