

## Passive transformations

$$(2) \quad \Phi' = \psi'^{\tilde{A}} \xi'_{\tilde{A}} = \psi^{\tilde{A}} \xi_{\tilde{A}} = \Phi$$

The object remains the same

If the spinor basis transforms according to

$$(3) \quad \xi'_{\tilde{A}} = \mathbf{R} \xi_{\tilde{A}} \mathbf{S} = L_{\tilde{A}}^{\tilde{B}} \xi_{\tilde{B}}$$

then the components must transform as

$$(4) \quad \psi'^{\tilde{A}} = \psi^{\tilde{B}} (L^{-1})_{\tilde{B}}^{\tilde{A}}$$

With respect to the new basis,  $\xi'_{\tilde{A}}$ , (new reference frame), the generalized spinor,  $\Phi$ , has transformed components.

From (2) – (4) we obtain

$$\psi^{\tilde{B}} (L^{-1})_{\tilde{B}}^{\tilde{A}} \xi'_{\tilde{A}} = \psi^{\tilde{B}} \mathbf{R}^{-1} \xi'_{\tilde{B}} \mathbf{S}^{-1} = \psi^{\tilde{B}} \xi_{\tilde{B}}$$

This is the **active transformation** of the object  $\psi^{\tilde{B}} \xi_{\tilde{B}}$ :

$$\psi^{\tilde{B}} \xi_{\tilde{B}} \rightarrow \psi^{\tilde{B}} \xi'_{\tilde{B}} = \psi^{\tilde{B}} \mathbf{R}^{-1} \xi_{\tilde{B}} \mathbf{S}^{-1}$$

This is equivalent to the active transformation of the object  $\psi^{\tilde{B}} \xi_{\tilde{B}}$

$$\psi^{\tilde{B}} \xi_{\tilde{B}} \rightarrow \psi^{\tilde{B}} \xi'_{\tilde{B}} = \psi^{\tilde{B}} \mathbf{R} \xi_{\tilde{B}} \mathbf{S}$$

Active transformations are thus embedded in passive transformations.